Exam Seat No:_

Enrollment No:____ **C.U.SHAH UNIVERSITY**

WADHWAN CITY University (Winter) Examination -2013

	<i>Cour</i> Dura	rse Name :B.ScSemester-I Subject Name: -Mathematics -I ation :- 2:30 Hours Date : 02/12/2013
	Insti (1) A (2) U (3) I (4)D (5) A	ructions:- Attempt all Questions of both sections in same answer book / Supplementary. Use of Programmable calculator & any other electronic instrument is prohibited. Instructions written on main answer Book are strictly to be obeyed. raw neat diagrams & figures (If necessary) at right places. Assume suitable & Perfect data if needed
		SECTION-I
Q1	a)	State Taylor's theorem.
	b)	If $y = e^x$, then $y_{16} = $
	c)	Center of the sphere $x^2 + y^2 + z^2 - 6x + 8y - 10z + 1 = 0$ is
	d)	If $y = \cos(ax + b)$, then find y_n .
	e)	Transform $\theta = 30^{\circ}$ in Cartesian form.
		$\lim_{x \to \infty} (1+x)^n - 1$
	f)	Prove that $x \to 0$ $x = n$.
		$a e^{x} - 2 b \cos x + 3 c e^{-x}$
Q2	a)	Find a, b, c so that $x \to 0$ $x \sin x$
	b)	State and prove Leibnitz's theorem.
	c)	Find the Maclaurin's expansion $f(x) = \sin x$.
02		$\lim_{x \to \infty} e^x + \log(1 - x) - 1$
Q2	a)	Evaluate: $x \to 0$ tan $x - x$.
	b)	Let $y = (x^2 - 2)^m$. Find the value of m such that
		$(x^2 - 2)y_{n+2} + 2x y_{n+1} - n(n+1)y_n = 0.$
	c)	Find y_n for $y = e^{-x} \cos x \sin 2x$.
Q3	a) b)	State and prove Lagrange's mean value theorem.
	0)	$r^2 - 2rdcas(\theta - a) + d^2 - a^2 = 0$ at point P and O. Then prove that $OP \cdot OO = d^2 - a^2$.
	c)	Show that following pair of spheres touch each other
	,	$x^2 + y^2 + z^2 = 64$, $x^2 + y^2 + z^2 - 12x + 4y - 6z + 48 = 0$.
03	9)	OR Lat two spheres he given by
QJ	<i>a)</i>	S ₁ = $x^2 + y^2 + z^2 + 2u_1x + 2v_1y + 2w_1z + d_1 = 0$, S ₂ = $x^2 + y^2 + z^2 + 2u_2x + 2v_2y + 2w_2z + d_2 = Then prove that S1 + \lambdaS2 = 0, where \lambda \in R, \lambda \neq -1, represents a family of spheres passing through the intersection of the spheres S1 = 0 and S2 = 0.$
	b)	In usual notation prove that polar equation of circle is
		$r^{2} + r_{1}^{2} - 2rr_{1}\cos(\theta - \theta_{1}) = a^{2}.$
	c)	Verify the Roll's theorem for the function $f(x) = x^2 - 2x + 3 = 5$
		$J (J) - \lambda = 2\lambda + J_J \lambda \in [0, 2].$

2

SECTION-II

Q4 a) What is the order and degree of
$$\left(\frac{dy}{dx}\right)^2 + 2\frac{dy}{dx} + xy = x^2$$
.
b) Define symmetric matrix.
c) Define scalar matrix.
d) Is the matrix $A = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$ in reduced row echelon form?
e) Is the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 5 & 3 \\ 1 & 0 & 0 \end{bmatrix}$.
(25 a) Find inverse of the matrix

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 5 \\ 1 & 0 & -3 \end{bmatrix}$$
.
(25 a) Find inverse of the matrix

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & -1 \\ 1 & 1 & 5 \\ 5 & 6 & 6 \\ 11 & 12 & 13 & -14 \\ 1 & 1 & 12 & 13 & -14 \\ 1 & 1 & 0 & -3 \end{bmatrix}$$
.
(25 a) Find normal form of the matrix

$$A = \begin{bmatrix} 3 & 4 & 5 & 6 \\ 1 & 1 & 1 & -1 \\ 1 & 1 & 5 \\ 5 & 6 & 6 \\ 11 & 12 & 13 & -14 \\ 1 & 12 & 13 & -14 \\ 1 & 10 & -3 \end{bmatrix}$$
.
(25 a) Find normal form of the matrix

$$A = \begin{bmatrix} 3 & 4 & 5 & 6 \\ 1 & 1 & -1 \\ 1 & 0 & -3 \end{bmatrix}$$
.
(26 a) Find eigen values and eigen vectors of
b) Solve the system by Gauss Jordan Method, for
(26 a) Find eigen values and eigen vectors of
(27 b) Solve the system by Gauss Jordan Method, for
(28 c) Solve the system by Gauss Jordan Method, for
(29 c) Solve the system by Gauss Jordan Method, for
(20 c) Solve the system by Gauss Jordan method
(26 a) Find eigen values and eigen vectors of
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(27 c) Solve: $\left(\frac{dy}{dx} + y \cot x = 4x \ cossec x$
(26 a) Verify Cayley — Hamilton theorem for
(27 b) Solve: $\left(\frac{dy}{dx} + y \cot x = 4x \ cossec x$
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(26 a) Verify Cayley — Hamilton theorem for
(27 b) Solve: $\left(\frac{dy}{dx} + x \right) \left(\frac{dy}{dx} + 2x \right) = 0$, where $p = \frac{dy}{dx}$.

*******2*******

Page **2** of **2**

2